## MATHEMATICAL SKILLS

## VOLUME OF A CUBE AND

## ASSOCIATED GEOMETRICAL SHAPES

## DESIGN AND TECHNOLOGY

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## HOW TO CALCULATE THE VOLUME OF A CUBE

DEFINITION: A cube is a solid object, composed of six equal squares, with a 90 degree angle between adjacent sides.


All the sides of a cube are the same measurement. There are two similar formulas for calculating a cube's volume.

## $\operatorname{VOLUME}(\mathrm{V})=\mathrm{A} \times \mathrm{A} \times \mathrm{A}$ ORA ${ }^{3}$

## EXAMPLE 1

If the measurement of one side is 100 mm :

## VOLUME $=100 \mathrm{~mm} \times 100 \mathrm{~mm} \times 100 \mathrm{~mm}$ VOLUME $=1000000 \mathrm{~mm}^{3}$ or $1000 \mathrm{~cm}^{3}$

## EXAMPLE 2

If the measurement of one side is 320 mm :
VOLUME $=320 \mathrm{~mm} \times 320 \mathrm{~mm} \times 320 \mathrm{~mm}$ VOLUME $=32768000 \mathrm{~mm}^{3}$ or $32768 \mathrm{~cm}^{3}$


# QUESTION 1 

What is the volume of the cube shown opposite?

## $\operatorname{VOLUME}(\mathrm{V})=\mathrm{A} \times \mathrm{A} \times \mathrm{A}$ OR $A^{3}$

If the measurement of one side is 90 mm :
VOLUME $=90 \mathrm{~mm} \times 90 \mathrm{~mm} \times 90 \mathrm{~mm}$
VOLUME $=729000 \mathrm{~mm}^{3}$ or $729 \mathrm{~cm}^{3}$

## QUESTION 2

What is the volume of the cube shown opposite?

$$
\begin{gathered}
\operatorname{VOLUME}(\mathrm{V})=\mathrm{A} \times \mathrm{A} \times \mathrm{A} \\
O R \mathrm{~A}^{3}
\end{gathered}
$$

If the measurement of one side is 120 mm :
VOLUME $=120 \mathrm{~mm} \times 120 \mathrm{~mm} \times 120 \mathrm{~mm}$ VOLUME $=1728000 \mathrm{~mm}^{3}$ or $1728 \mathrm{~cm}^{3}$

## QUESTION 3

What is the volume of the cube shown opposite?

## $\operatorname{VOLUME}(\mathrm{V})=\mathrm{A} \times \mathrm{A} \times \mathrm{A}$ OR $A^{3}$

If the measurement of one side is 55 mm :
VOLUME $=55 \mathrm{~mm} \times 55 \mathrm{~mm} \times 55 \mathrm{~mm}$
VOLUME $=166375 \mathrm{~mm}^{3}$ or $166.375 \mathrm{~cm}^{3}$


## QUESTION 1

What is the volume of the cube shown opposite?
$\operatorname{VOLUME}(\mathrm{V})=\mathrm{A} \times \mathrm{A} \times \mathrm{A}$ OR A ${ }^{3}$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## QUESTION 2

What is the volume of the cube shown opposite?
$\operatorname{VOLUME}(\mathrm{V})=\mathrm{A} \times \mathrm{A} \times \mathrm{A}$ OR A ${ }^{3}$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

## QUESTION 3

What is the volume of the cube shown opposite?

$$
\begin{gathered}
\operatorname{VOLUME}(\mathrm{V})=A \times A \times A \\
O R A^{3}
\end{gathered}
$$

## EXAM QUESTION - CUBE



A solid cube of aluminium (A) has 200 mm sides. However, a smaller area in the form of a cube with 100 mm length sides, has been machined from the top surface (B).
What is the volume of the finished 3D shape?
How to work out the answer:
Start by treating both $A$ and $B$ as solid cubes.
Work out the volume of each cube $A$ and $B$

## CUBE 'A'

If the measurement of one side is 200 mm :
VOLUME $=200 \mathrm{~mm} \times 200 \mathrm{~mm} \times 200 \mathrm{~mm}$ VOLUME $=8000000 \mathrm{~mm}^{3}$ or $8000 \mathrm{~cm}^{3}$

CUBE 'B'
If the measurement of one side is 100 mm :
VOLUME $=100 \mathrm{~mm} \times 100 \mathrm{~mm} \times 100 \mathrm{~mm}$
VOLUME $=1000000 \mathrm{~mm}^{3}$ or $1000 \mathrm{~cm}^{3}$

Then, subtract the volume of B away from the volume of $A$, to find the final overall volume

FINAL VOLUME $=\mathrm{A}-\mathrm{B}$
FINAL VOLUME $=8000000 \mathrm{~mm}^{3}-1000000 \mathrm{~mm}^{3}$
FINAL VOLUME $=7000000 \mathrm{~mm}^{3}$ or $7000 \mathrm{~cm}^{3}$

## EXAM QUESTION - CUBE



A solid cube of aluminium (A) has 200mm sides. However, a smaller area in the form of a cube with 100 mm length sides, has been machined from the top surface (B).
What is the volume of the finished 3D shape? Explain your working out.

## EXAM QUESTION - CUBE



The unusual solid geometrical shape shown opposite can be treated as two cubes.

Calculate the entire volume of the shape/form.

Explain your working out.

The measurement of a side of cube $A$ is clearly shown as 150 mm
To work out the length of one side of cube B, simply subtract 150 mm from the overall height of the shape.

225mm (overall height) - 150 mm (length of one side of cube A)
$225 m m-150 \mathrm{~mm}=75 \mathrm{~mm}$ (this is the length of one side of cube $B$ )

Then work out the volume of cubes $A$ and $B$

## CUBE 'A'

If the measurement of one side is 150 mm :

$$
\begin{array}{ll}
\text { VOLUME }=150 \mathrm{~mm} \times 150 \mathrm{~mm} \times 150 \mathrm{~mm} & \text { VOLUME }=75 \mathrm{~mm} \times 75 \mathrm{~mm} \times 75 \mathrm{~mm} \\
\text { VOLUME }=3375000 \mathrm{~mm}^{3} \text { or } 3375 \mathrm{~cm}^{3} & \text { VOLUME }=421875 \mathrm{~mm}^{3} \text { or } 421.875 \mathrm{~cm}^{3}
\end{array}
$$

Then, add the volume of cube B with the volume of cube $A$, to find the final overall volume

FINAL VOLUME $=\mathrm{A}+\mathrm{B}$
FINAL VOLUME $=3375000 \mathrm{~mm}^{3}+421875 \mathrm{~mm}^{3}$
FINAL VOLUME $=3796875 \mathrm{~mm}^{3}$ or $3796.875 \mathrm{~cm}^{3}$

## EXAM QUESTION - CUBE



The unusual solid geometrical shape shown opposite can be treated as two cubes.

Calculate the entire volume of the shape/form.

Explain your working out.

